

# Correction Methods for Neutron Imaging on the Basis of Monte-Carlo Simulations

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*The content is part of the PhD thesis of R. Hassanein*

# Outline

- Introduction: the problem in quantification → scattering
- Setup of the transmission experiment
- Monte-Carlo model: The Point-Scattered Function approach
- Parameters and relevant data
- Correction tool: QNI
- Results of practical applications
- Outlook: further improvements

# Water Distribution in Limestones

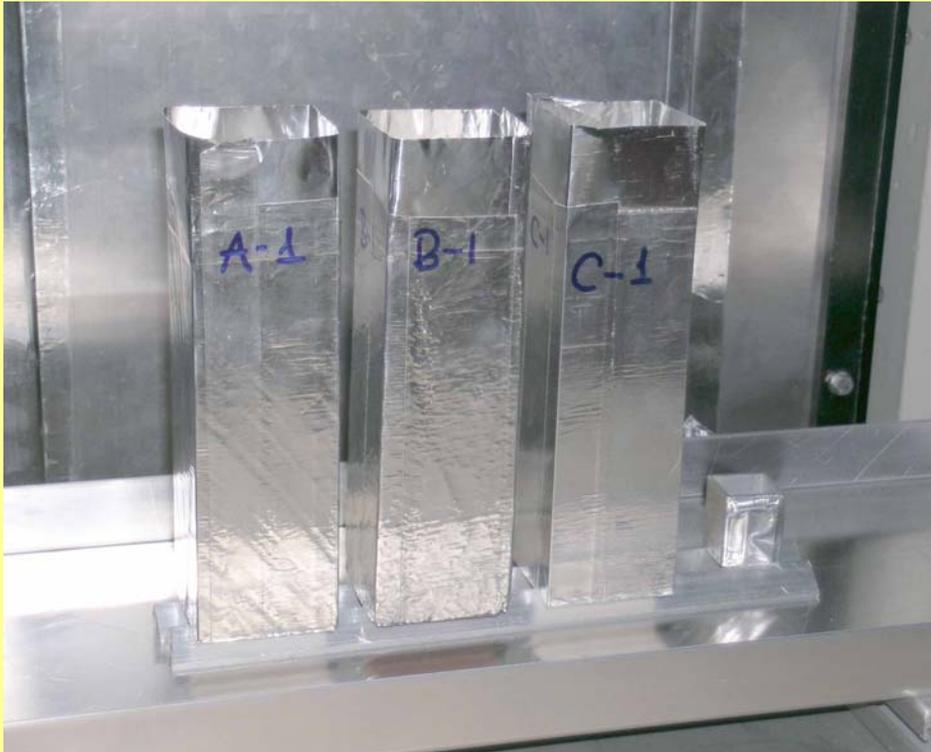


**Porous Salem Limestone**  
(*'the'* Indiana Limestone;  
a coarse-grained  
stone of calcite)

**Mansfield Sandstone**  
(a red stone with  
relatively coarse  
grains)

**Hindustan Whetstone**  
(a siltstone with angular,  
fine-grained quartz  
and feldspars)

# Experimental Setup



Absorption of water in **upward direction**  
(Prof. H.O. Meyer, Indiana University)

Aluminum cover to  
prevent evaporation from surface

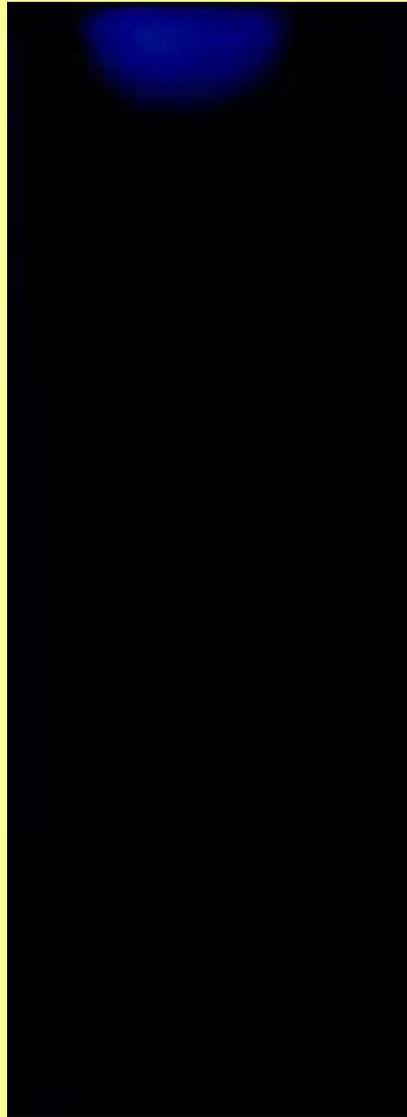


Absorption of water  
in **downward direction**

sealing and surfaces  
treated with silicon

# Water migration in sandstones radiography

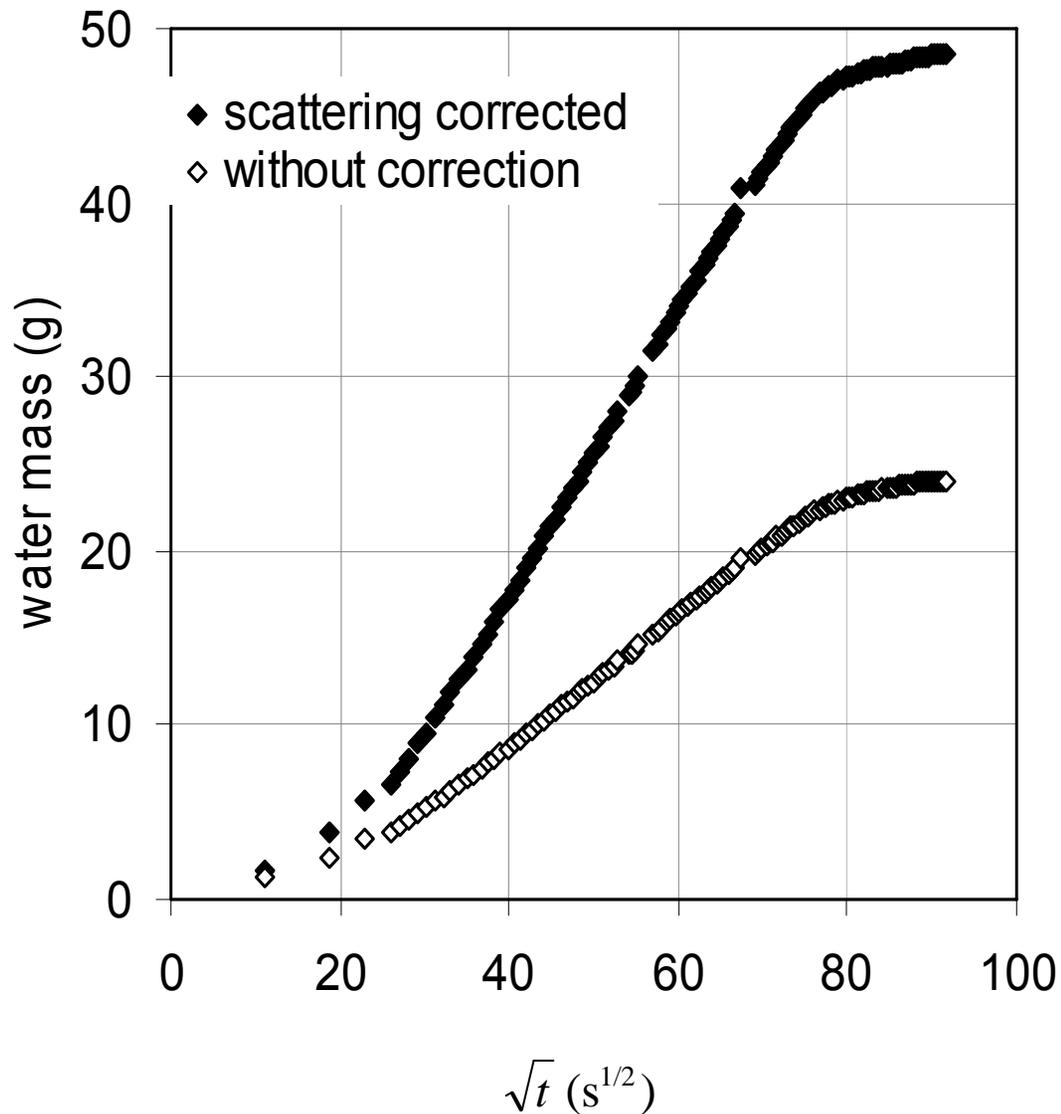
downward  
flooding



upward  
soaking



# Water migration in sandstones

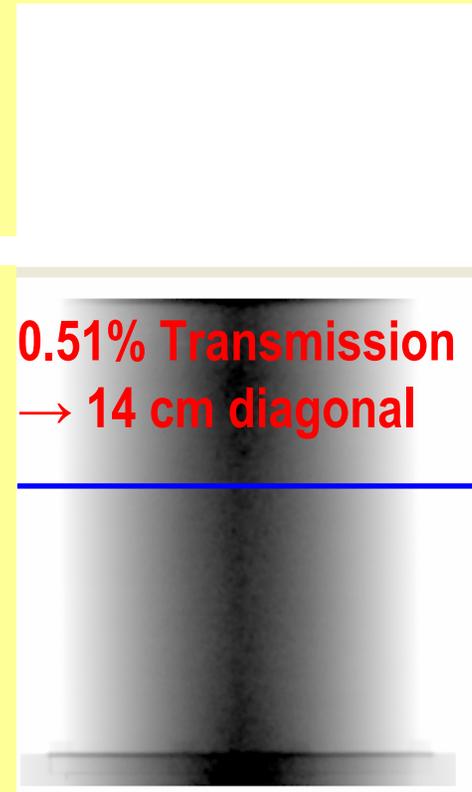
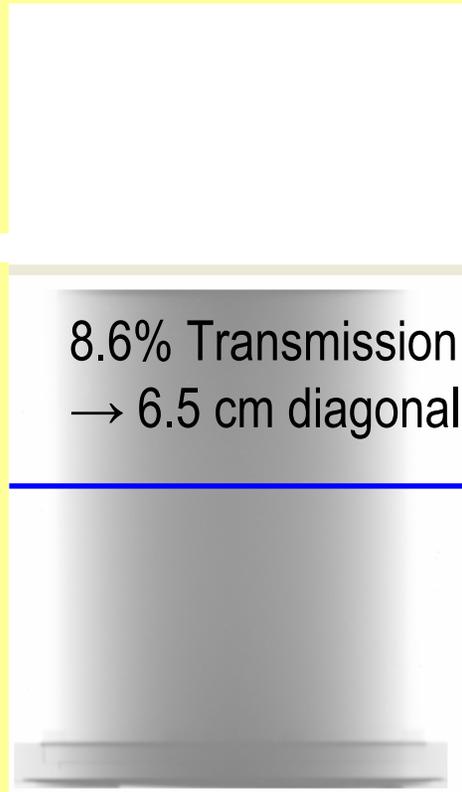
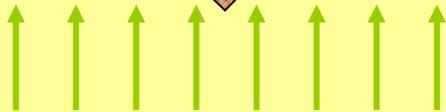
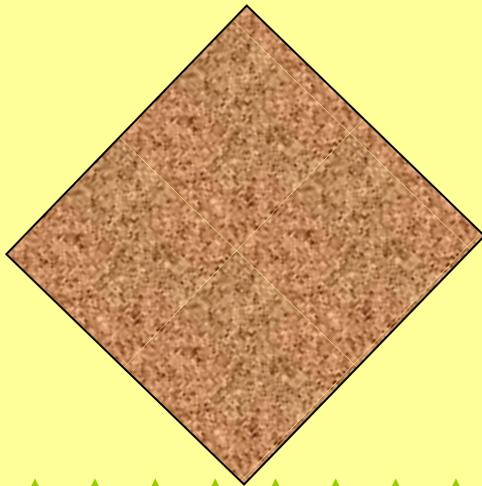


*The error in the quantification can be up to 100%!*

# Water Content in Sand Columns -tomography-

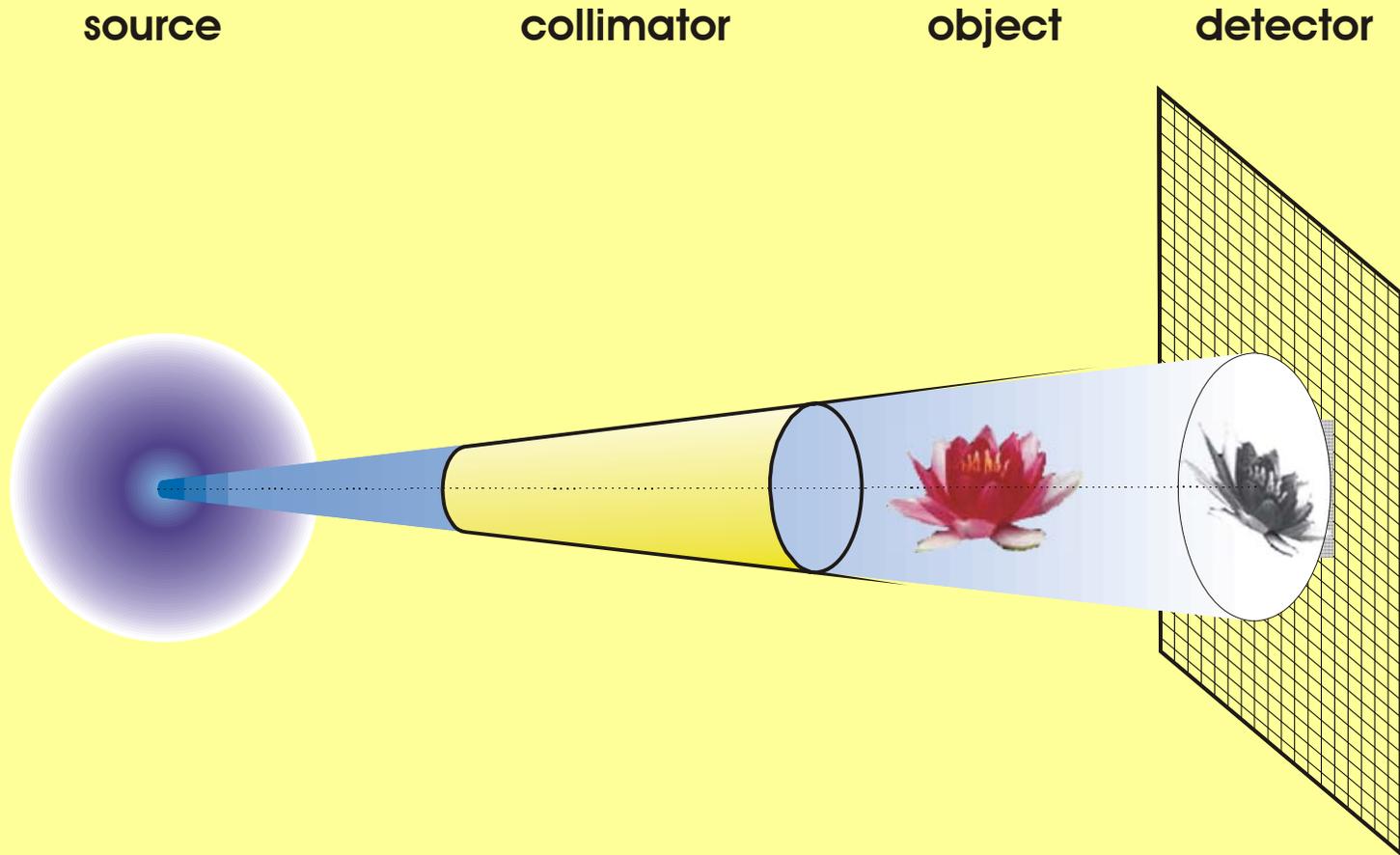
45° view: before

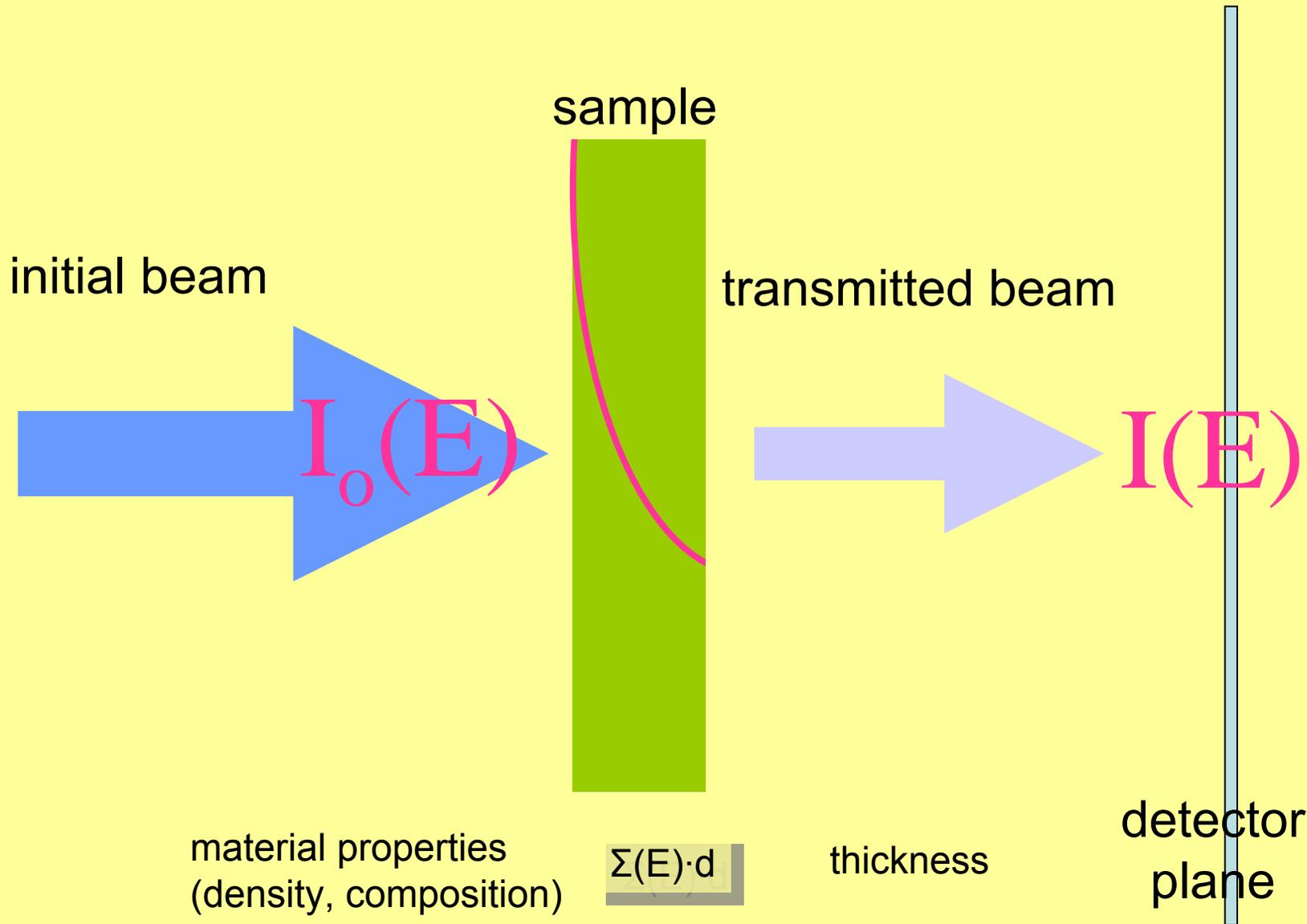
after correction



# The principle

## Simplified setup for radiographic studies





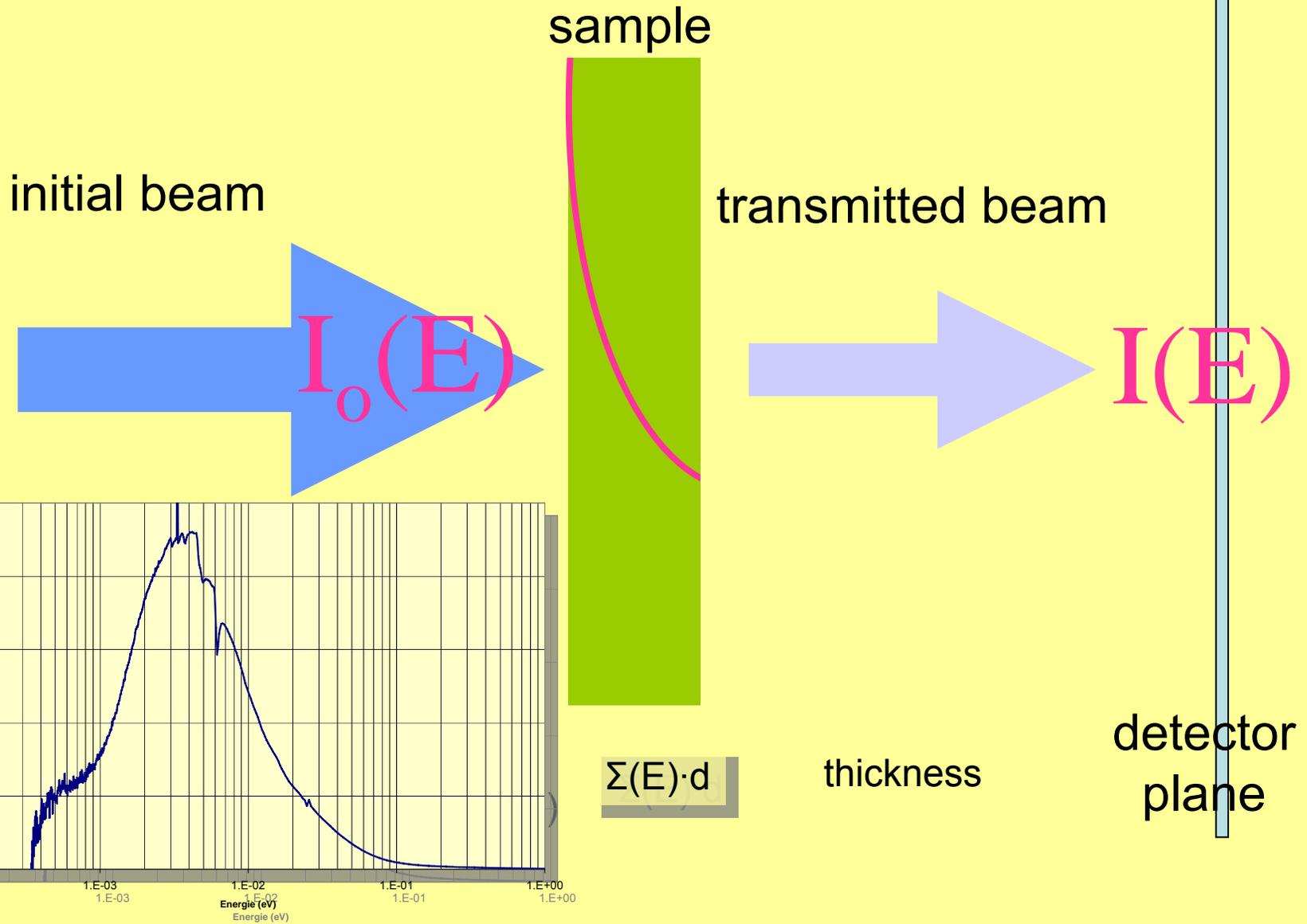
# Approach for quantification

(also in use for tomography)

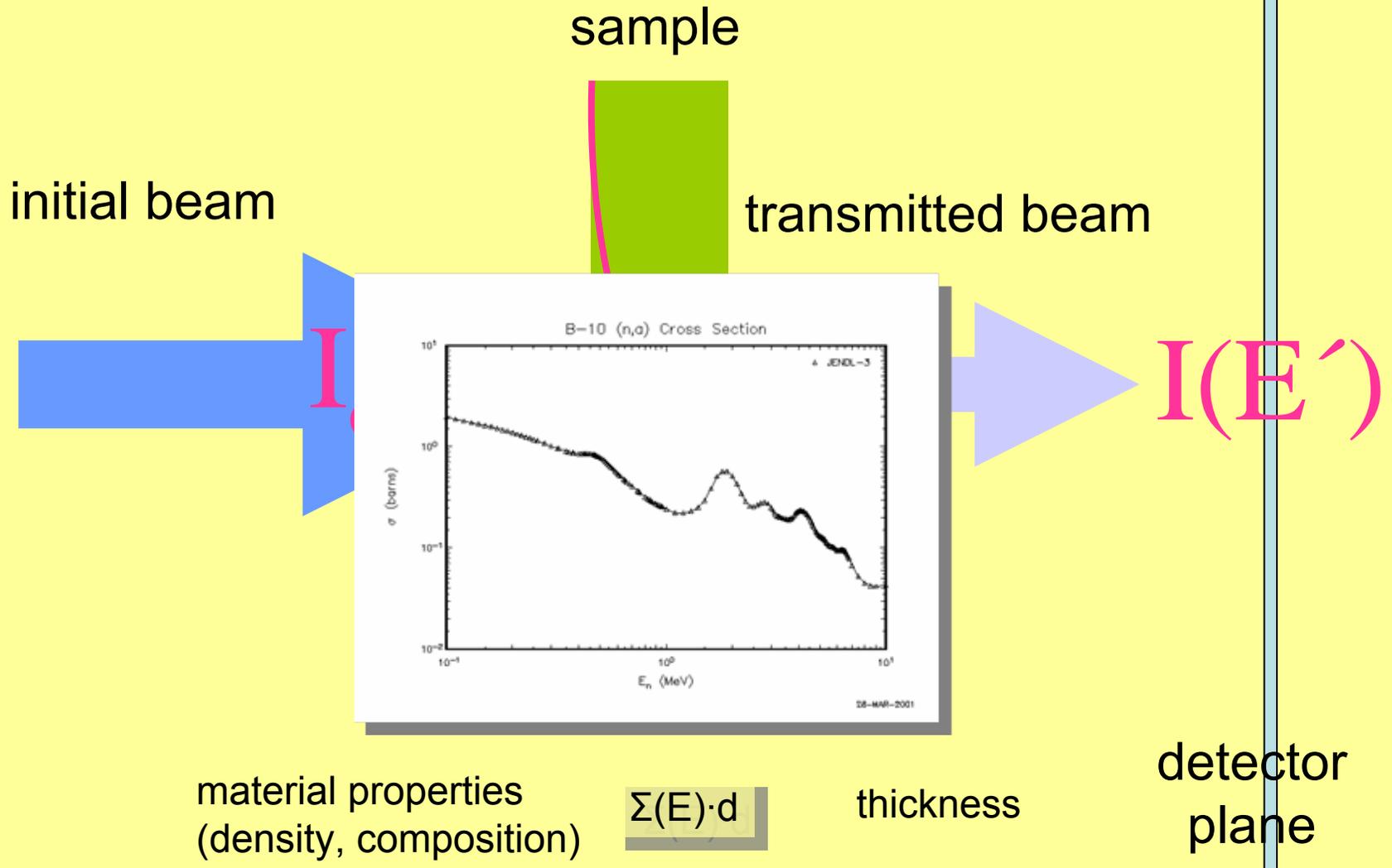
$$I(E') = I_0(E) \cdot e^{-\Sigma(E) \cdot d}$$

- Assumed, the intensities  $I_0$  and  $I$  are measured precisely:
- The *sample thickness*  $d$  can be obtained, if the material composition is known
- The *material properties*  $\Sigma$  can be obtained, if the sample thickness is known

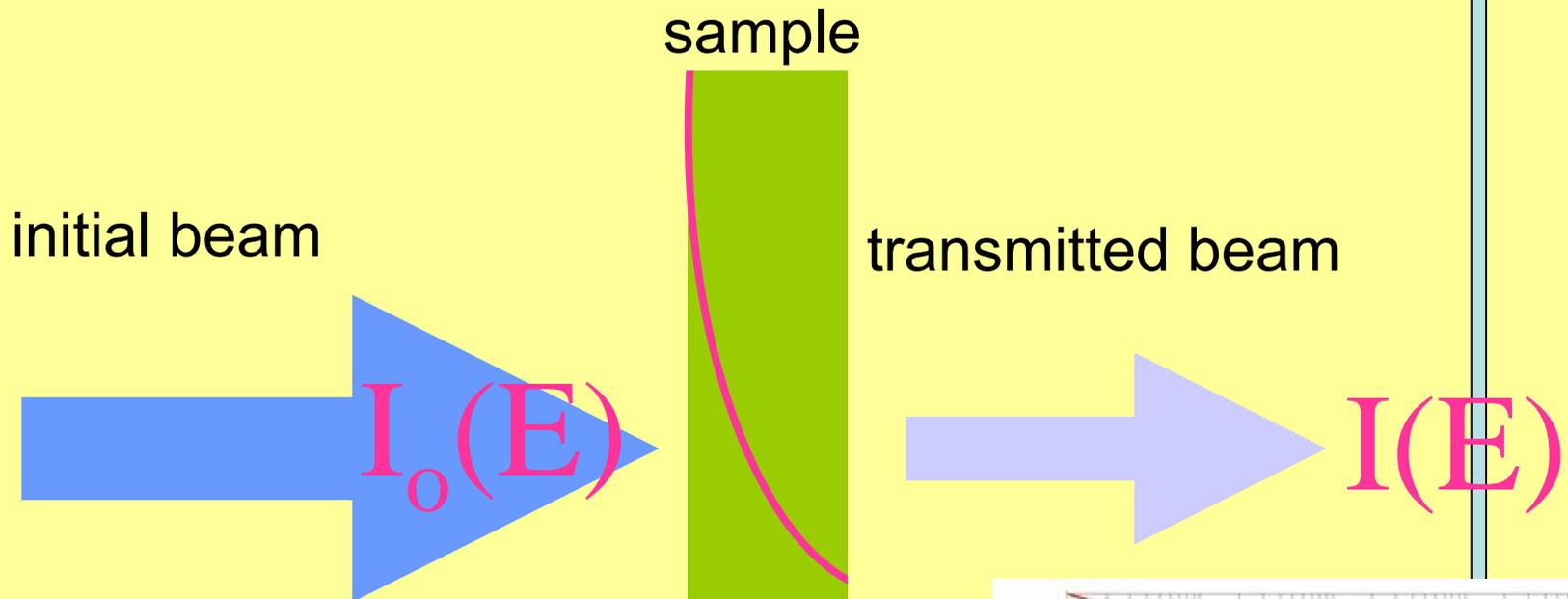
**Problem 1:** The initial beam has a spectral distribution (about a Maxwellian)



**Problem 2:** The sample cross-section  $\Sigma$  is energy dependent, modifying the transmitted spectrum

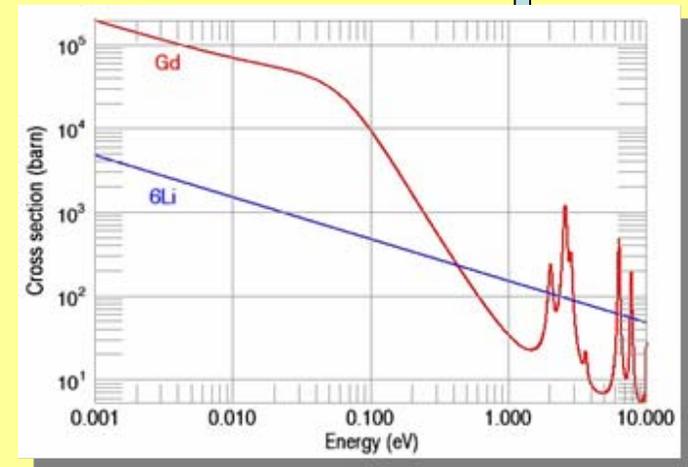


**Problem 3:** The detector has an energy dependent response, weighting the neutrons differently

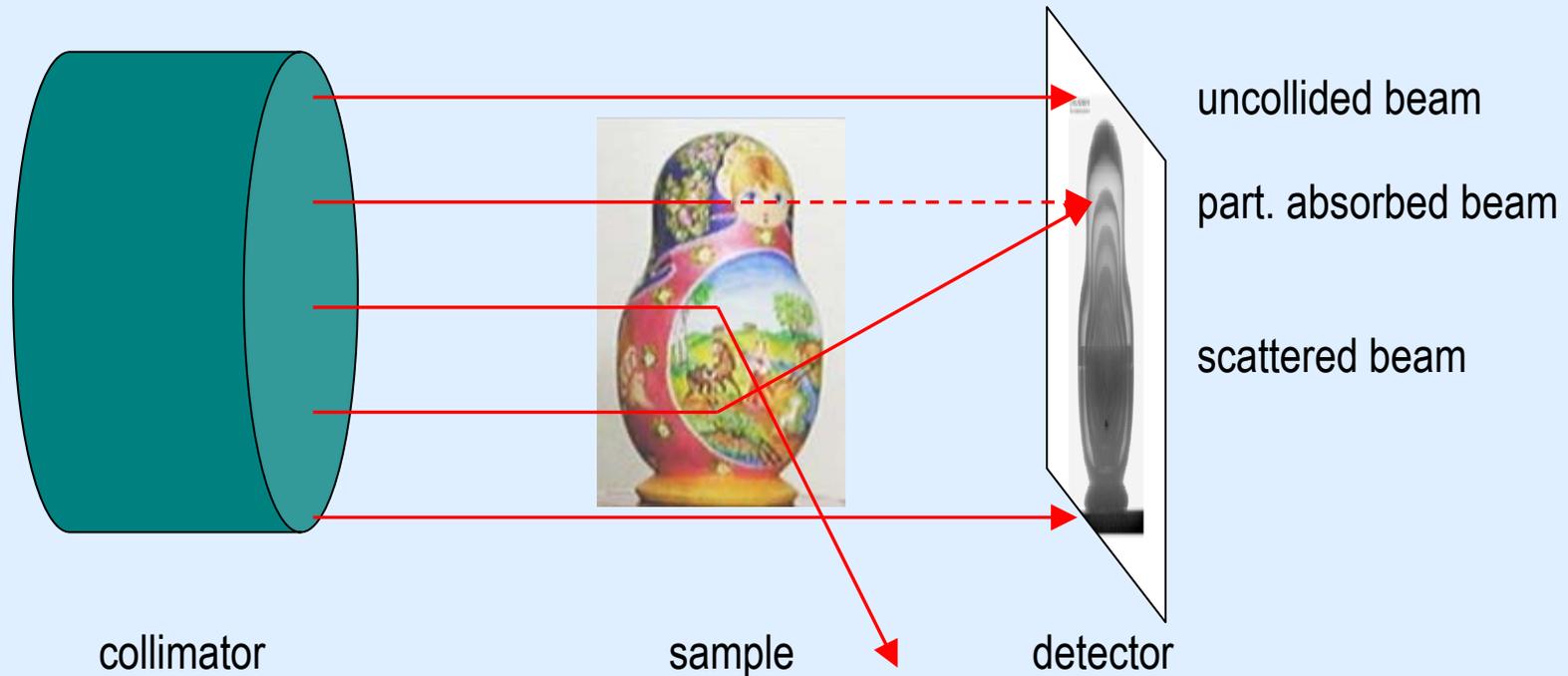


material properties  
(density, composition)

$$\Sigma(E) \cdot d$$



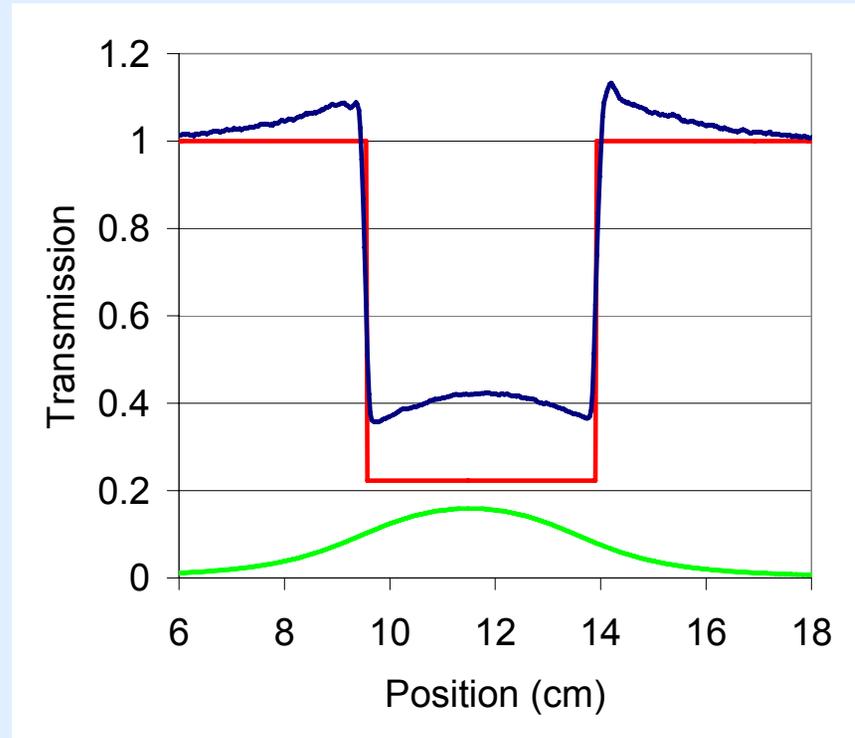
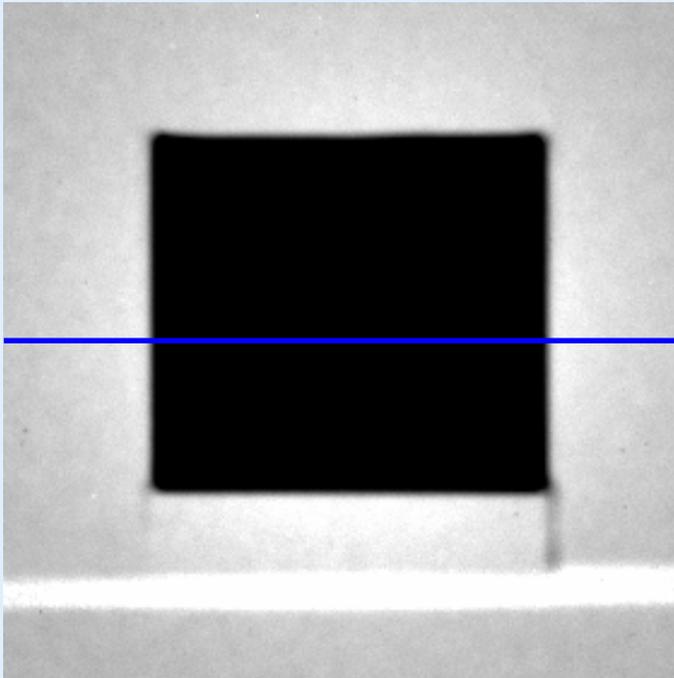
**Problem 4:** The transmitted beam is “contaminated”  
by diffuse scattered neutrons



The scattering pretends a higher transmission value behind the sample, which is mistaken for less mass thickness.

# Skyshine by the Sample Scattering

Radiograph of 5 mm water in 2 cm distance to the detector with a horizontal profile



# Monte Carlo Approach

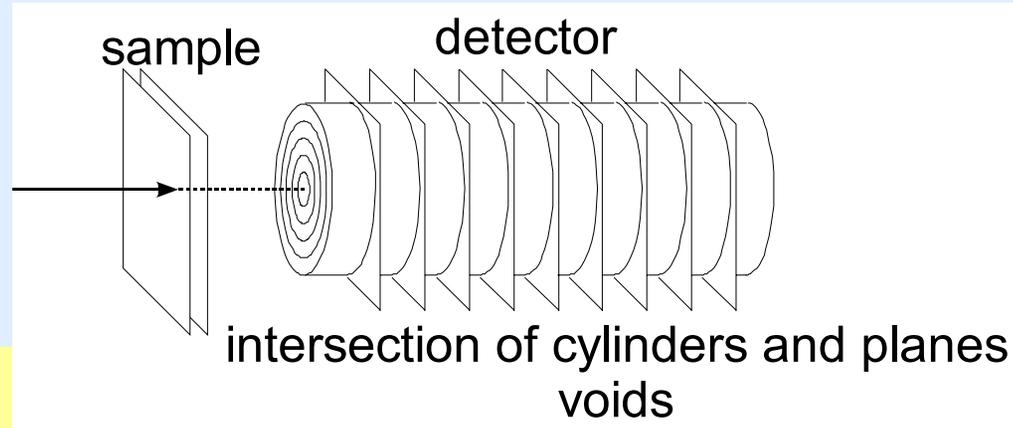
- MCNPX is able to simulate all details of the transmission process
- This enables to consider all effects of neutron interaction with sample and detector
- The processes are separable into the transmitted and scattered component, defining the Point Scattered Function (PScF)
- The cross-section data are within the embedded data libraries of the code (some need for modification was identified)
- The F1 tally was used mainly

# Simulation of the Point Scattered Function

The PScF is simulated by the **Monte-Carlo software MCNPX**.

The main parameters are:

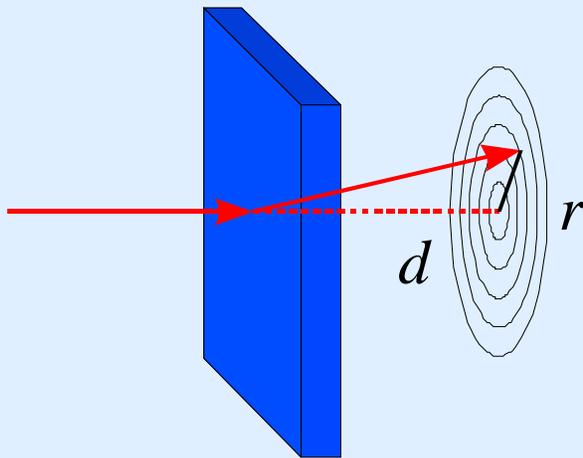
- sample composition
- sample thickness
- energy spectrum of the neutron source, beam geometry
- detector material and thickness (energy sensitivity)
- sample – detector distance



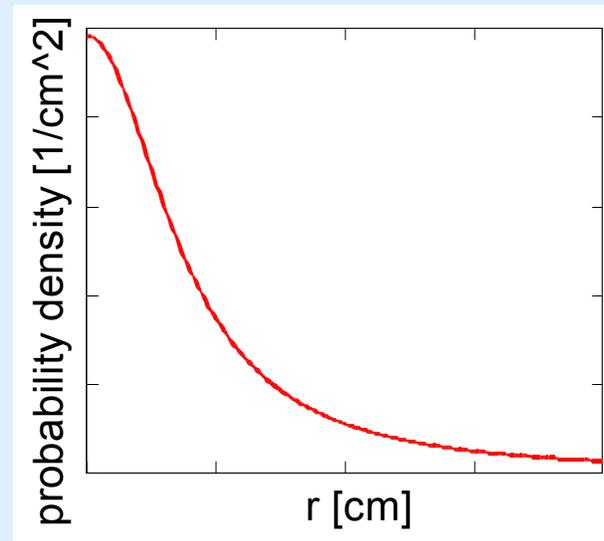
# Correction of the Sample Scattering

Computation and subtraction of the sample scattering

The sample scattering is computed based on “**Point Scattered Functions**” (PScF).



point source  $I_0$       sample layer



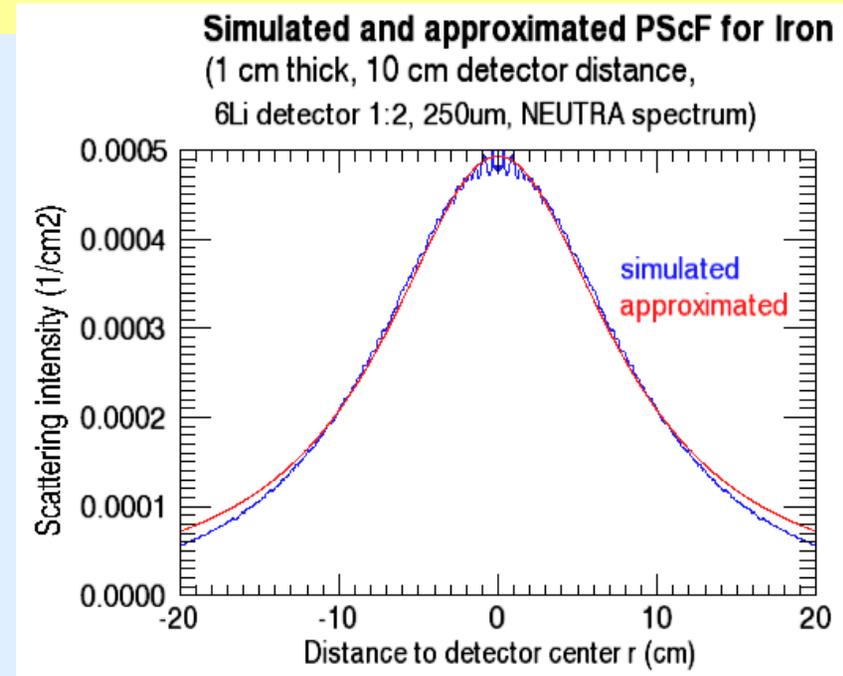
point scattered function

# Approximation of the PScF

Since the simulated PScF are noisy and are obtained for discrete sample thicknesses, detector distances and pixel sizes, an **approximation is necessary for the arbitrary values of a real experiment.**

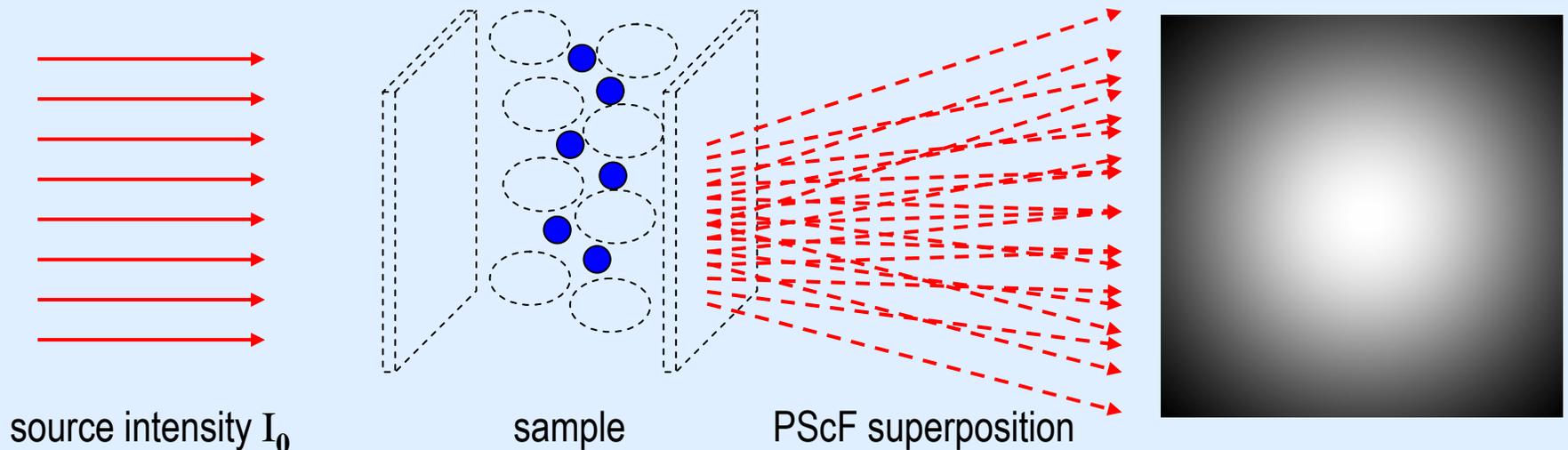
The approximation is based on isotropic scattering:

$$PScF_{Approximation}(r) = S_A \cdot \frac{d_A}{4\pi(d_A^2 + r^2)^{3/2}}$$



# Computation of the Sample Scattering

The total sample scattering is the **superposition of the corresponding PScF**, where each point\* of the sample can have its own PScF (corresponding to the detector distance, sample material and transmitted thickness).



\* "point" = group of about  $4 \times 4$  pixels (depending on the image size) because of the computation time  $\sim (\text{group width})^4$

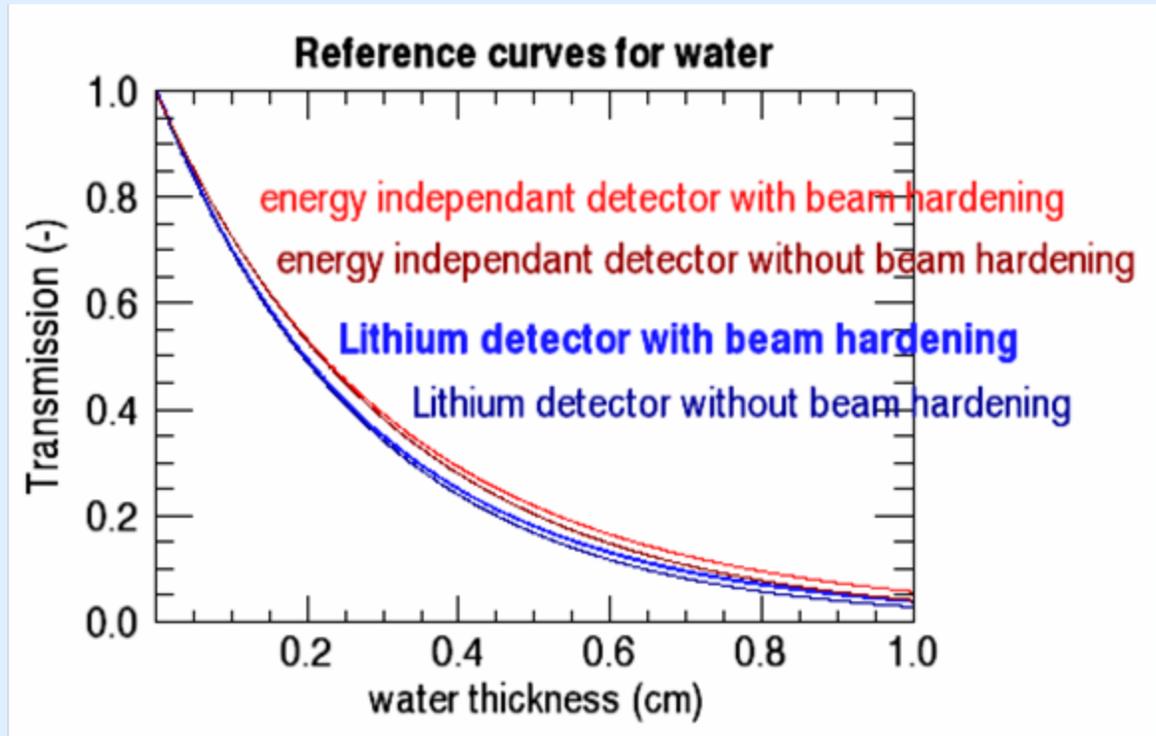
# Iterative Algorithm

- **Corrected transmission image = radiography – sample scattering**
- With the corrected image, a more precise base for the choice of the PScF is available and the computation is repeated.
- After about 4 iterations the algorithm converges in the range of  $\pm 1$  %.

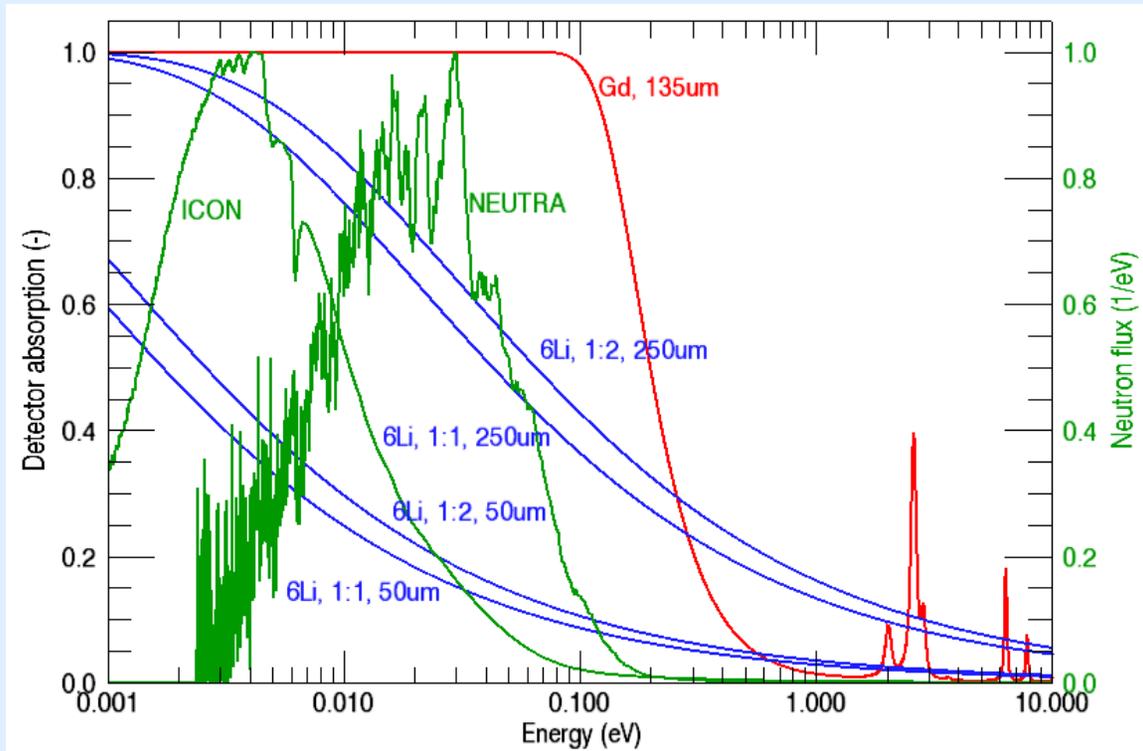
# Correction of the Spectral Effects

The Monte-Carlo simulations of the PScF provide also **reference curves** for the correction of the

- beam hardening
- energy dependent detector sensitivity



# Detector Absorption Rates



Detector absorption rate:  $A(E) = 1 - \exp(-\Sigma_{\text{detector}}(E) \cdot t_{\text{detector}})$

# Effective Cross Section

Cross section of 2 mm water for the different detectors:

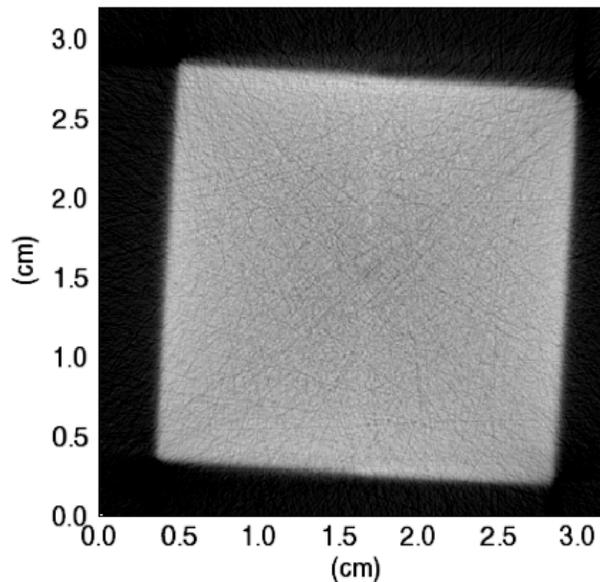
$$\Sigma_{\text{eff, H}_2\text{O}} = \frac{-1}{t_{\text{H}_2\text{O}}} \cdot \ln \frac{\int I(E) \cdot \exp(-\Sigma_{\text{H}_2\text{O}}(E) \cdot t_{\text{H}_2\text{O}}) \cdot A(E) dE}{\int I(E) \cdot A(E) dE}$$

detector	NEUTRA $\Sigma_{\text{eff}} (1/\text{cm})$	ICON $\Sigma_{\text{eff}} (1/\text{cm})$
Gd, 135 $\mu\text{m}$	3.29	4.11
$^6\text{Li}$ , 1:2, 250 $\mu\text{m}$	3.40	4.20
$^6\text{Li}$ , 1:1, 250 $\mu\text{m}$	3.42	4.27
$^6\text{Li}$ , 1:2, 50 $\mu\text{m}$	3.51	4.62
$^6\text{Li}$ , 1:1, 50 $\mu\text{m}$	3.52	4.65

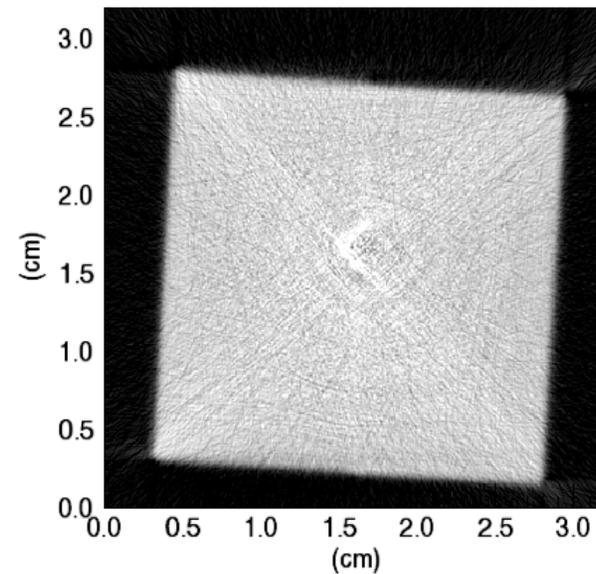
# Correction of Tomograms

For tomograms **each projection is corrected** in a pre-processing step.  
(The change of the sample geometry and detector distance in each projection must be considered)

**horizontal slice of an iron cube (side length 2.5 cm)**



uncorrected

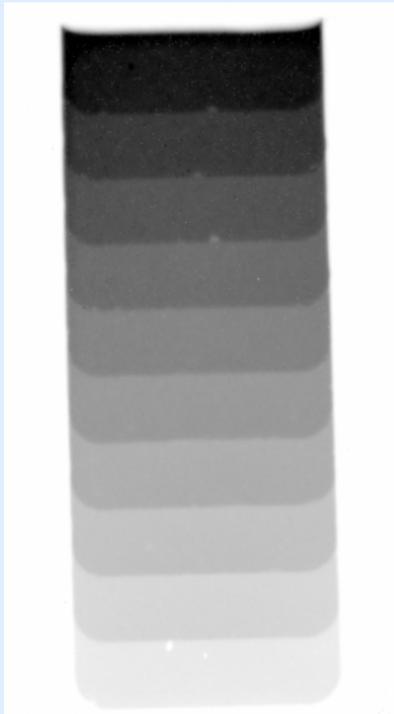


corrected

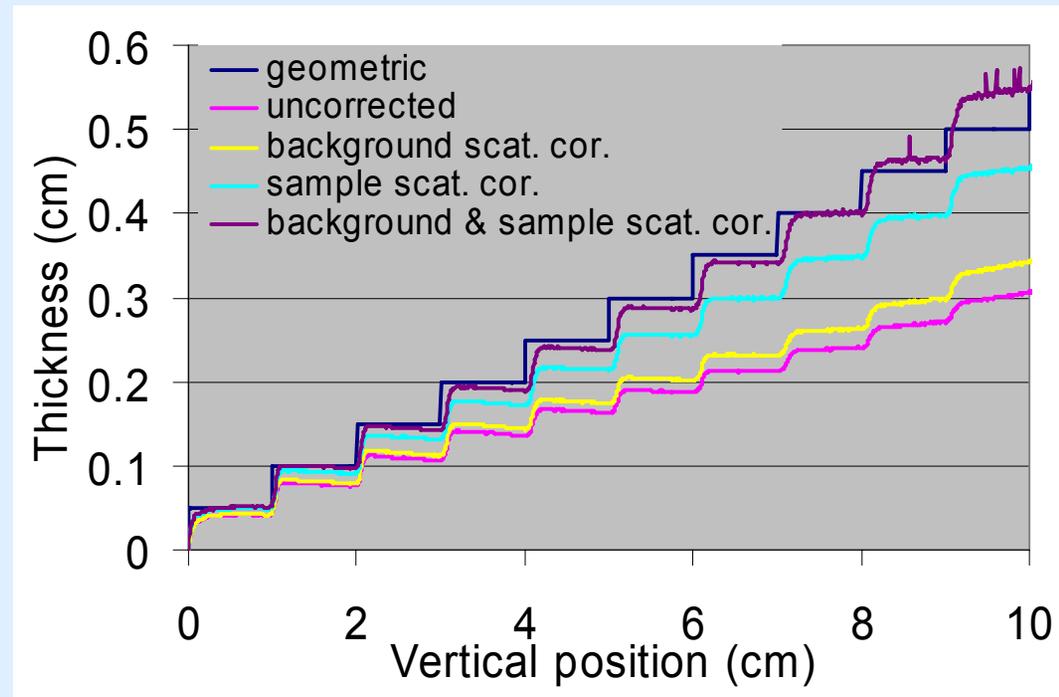
# Application 1

## Experiments at ANTARES, FRM-II Munich

Example water steps: size 4×10 cm, thickness 0.5–5.0 mm, detector distance 4 cm



corrected radiography

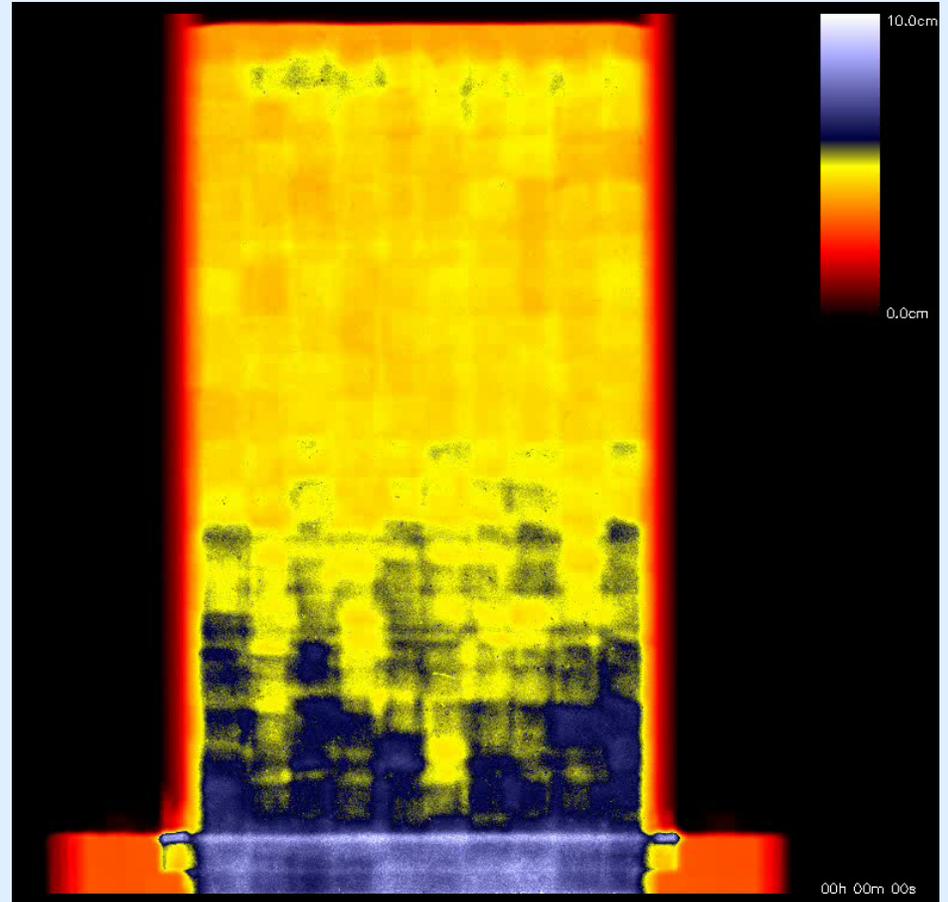
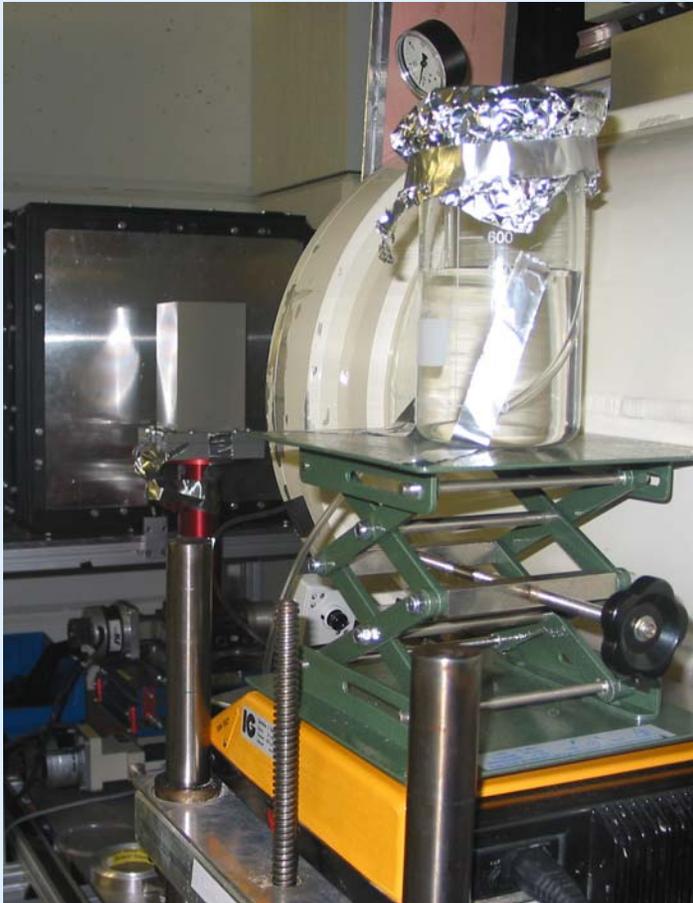


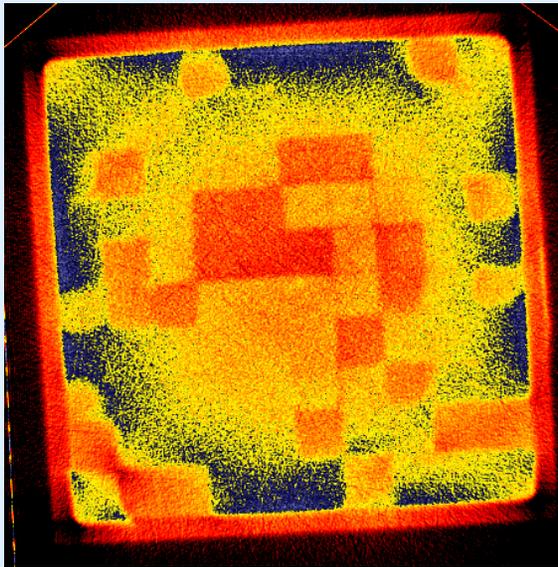
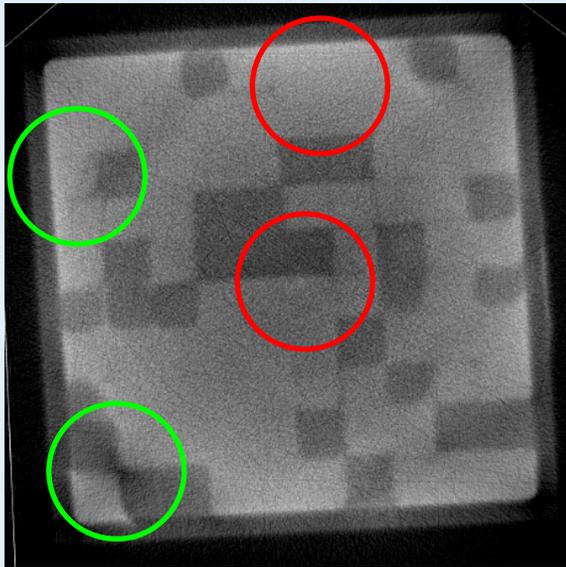
remaining error  $\leq 5\%$

# Application 2

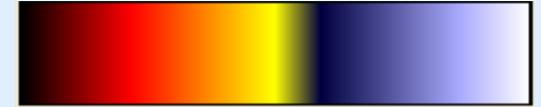
## Imbibition and Drainage of Sand Columns with D<sub>2</sub>O

(Experiment: I. Neuweiler, M. Vasin, P. Lehmann, Univ. Stuttgart & ETH Zurich)

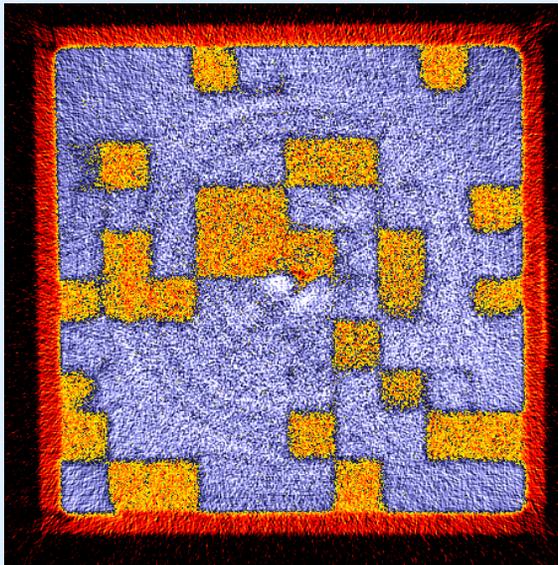
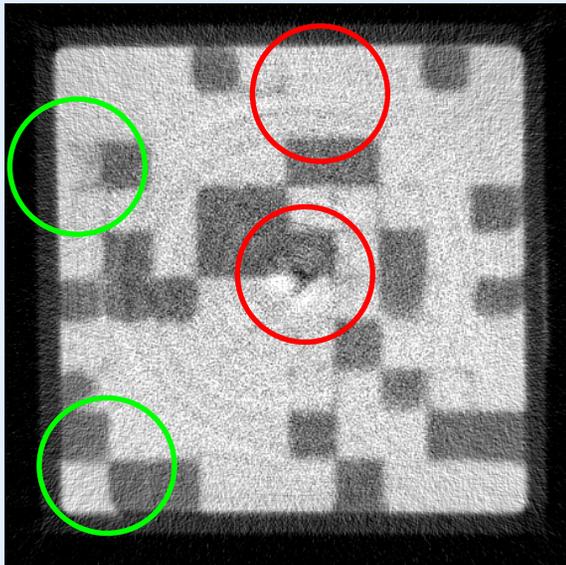




uncorrected slice



void Al sand water



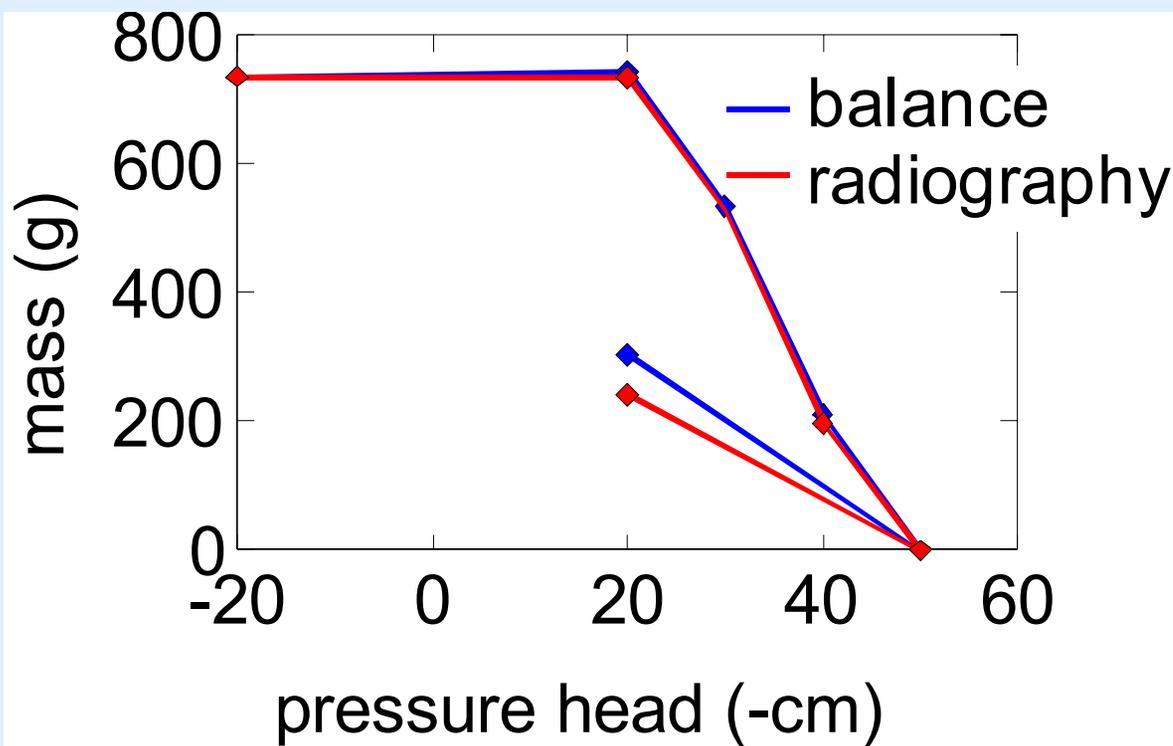
corrected slice

- more noise
- more artefacts

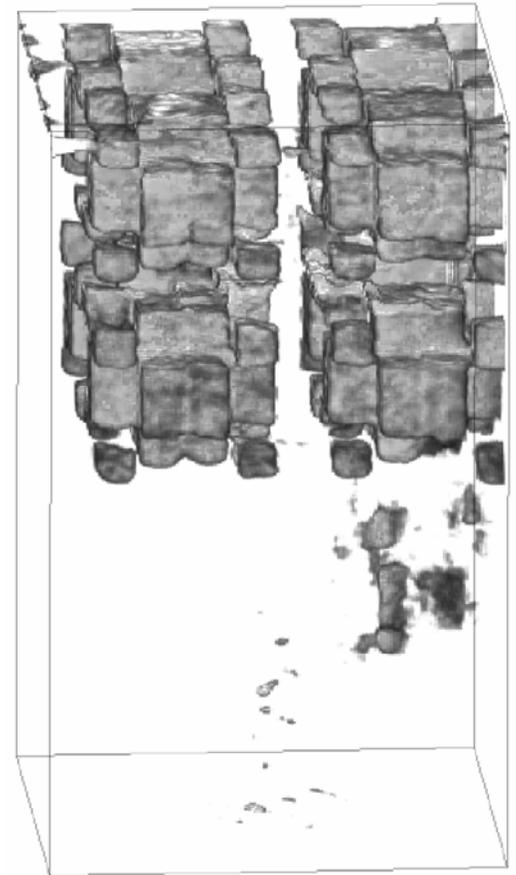
- + less blurring
- + more details

+ **correct**  
**attenuation values**

# Imbibition and Drainage of Sand Columns with D<sub>2</sub>O



remaining error  $\leq 5\%$



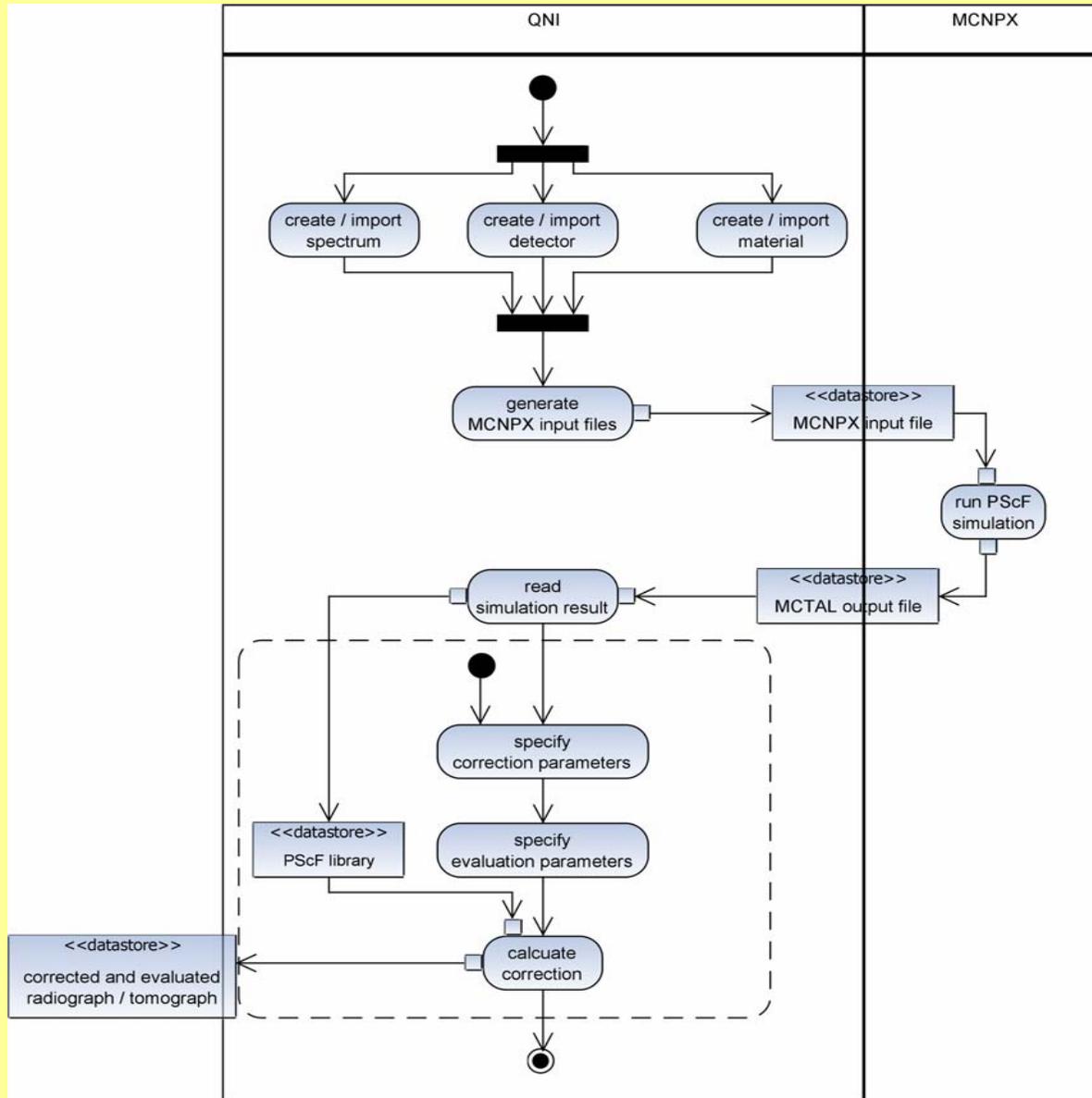
# Conclusions

- Neutron radiography (NR) is suitable method for **quantitative**, non-destructive investigations with an accuracy of  $\sim 5\%$ , depending on the material combination.
- An **appropriate experimental setup** is decisive (facility, material, dimensions, detector system)
- The **properties of the NR facility** must be known (energy spectrum, detector)
- **Monte-Carlo simulations** are a valuable tool for the investigation of effects in NR (e.g. scattering, beam hardening, detector efficiency)
- A “**user friendly**” **implementation** of the correction algorithm allows to use the correction methods in the daily work and improve the results.

# Outlook

- QNI – the correction tool written in IDL
- Improved experimental conditions
- Further approaches needs considerations (cold neutron imaging, energy selective studies)

# QNI – the correction tool



## Work-flow

- Based on PhD work of **René Hassanein**
- Programmed in IDL
- Available for other users in October 2006

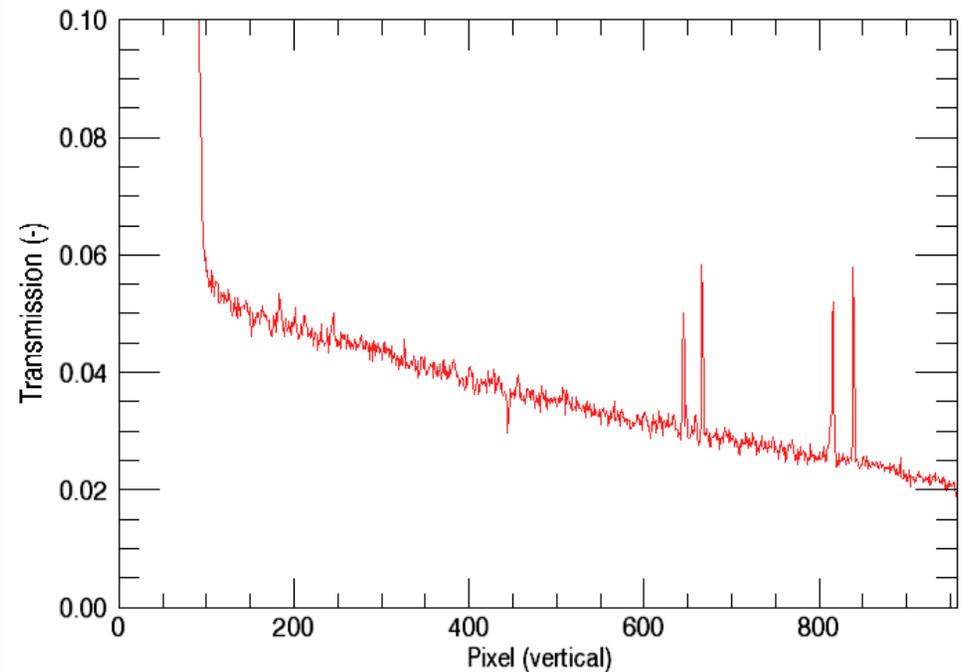
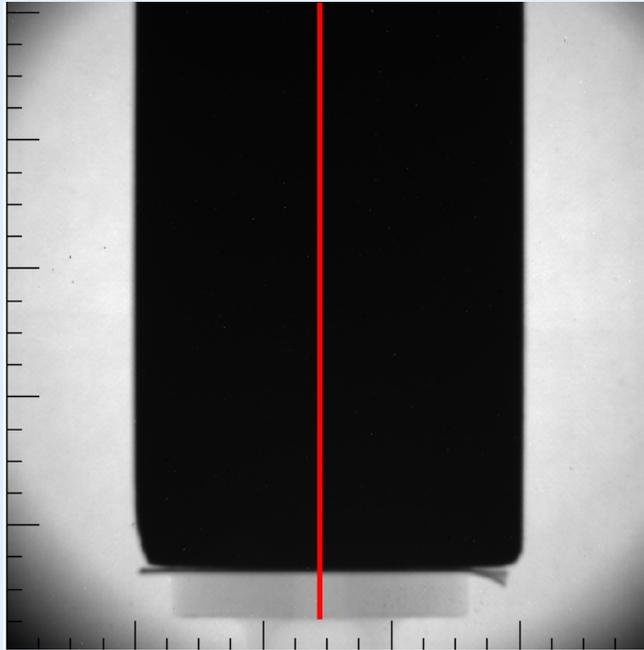
# Avoiding Background Scattering: Beam Delimiters

Beam limitations in order to avoid scattering sources:

- aperture at the front position
- aperture at the collimator exit
- limitation of the field of view (figure)



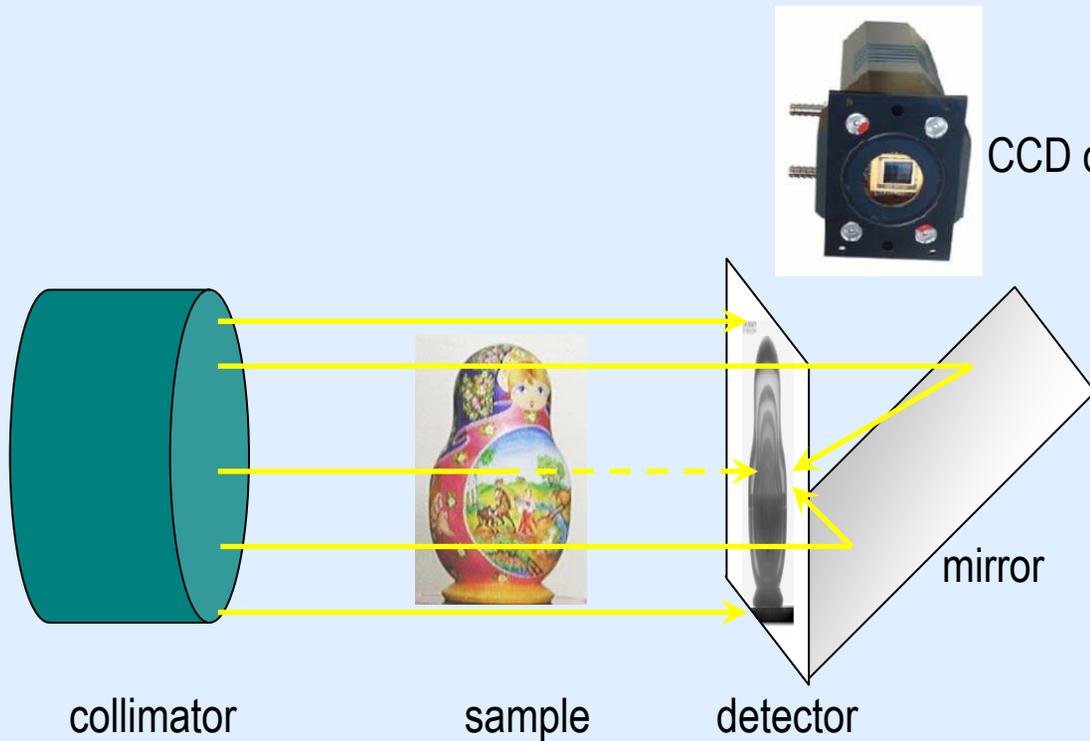
# Recording of the Background Scattering



Measurement of the scattering behind a black body:

- not constant
- to be scaled

# Distortion by Scattering at the Experimental Setup



Neutrons are scattered by the surrounding of the sample (e.g. camera box and shielding) and pretend again high transmission and **less mass thickness**.

# Experiments at the Bragg edges of the materials → Improvement of the data base in MCNPX

